CSC 222: Computer Organization & Assembly Language

2 – Data Representation

Instructor: Mr. Farooq Faisal
ICS & IT FMCS The University of Agriculture Peshawar

Number System

- Any number system using a range of digits that represents a specific number. The most common numbering systems are decimal, binary, octal, and hexadecimal.
- Numbers are important to computers
  - represent information precisely
  - can be processed
- For example:
  - to represent yes or no: use 0 for no and 1 for yes
  - to represent 4 seasons: 0 (autumn), 1 (winter), 2(spring) and 3 (summer)

Positional Number System

- A computer can understand positional number system where there are only a few symbols called digits and these symbols represent different values depending on the position they occupy in the number.

- A value of each digit in a number can be determined using
  - The digit
  - The position of the digit in the number
  - The base of the number system (where base is defined as the total number of digits available in the number system).

Decimal Number System

- A numbering system that uses ten digits, from 0 to 9, to represent numerical values/quantities. Each digits has a weighted value of $10^0, 10^1, 10^2, 10^3$ and so on, ranging from right to left.

Binary Number System

- A numbering system that uses two digits 0 and 1, to represent numerical values/quantities. Each digits has a weighted value of $2^0, 2^1, 2, 2^3$ and so on, ranging from right to left.

Hexadecimal Number System

- A numbering system that uses sixteen digits, from 0 to 9 and A to F, to represent numerical values/quantities. Each digits has a weighted value of $16^0, 16^1, 16^2, 16^3$ and so on, ranging from right to left.

Conversion Between Number Systems

- <u>Converting Hexadecimal to Decimal</u>
- Multiply each digit of the hexadecimal number from right to left with its corresponding power of 16.
- Convert the Hexadecimal number **82ADh** to decimal number.

Conversion Between Number Systems

- <u>Converting Binary to Decimal</u>
- Multiply each digit of the binary number from right to left with its corresponding power of 2.
- Convert the Binary number **11101** to decimal number.

Conversion Between Number Systems

- Converting Decimal to Binary
- Divide the decimal number by 2.
- Take the remainder and record it on the side.
- REPEAT UNTIL the decimal number cannot be divided into anymore.

Conversion Between Number Systems

- Converting Decimal to Hexadecimal
- Divide the decimal number by 16.
- Take the remainder and record it on the side.
- REPEAT UNTIL the decimal number cannot be divided into anymore.

Conversion Between Number Systems

- ## Converting Hexadecimal to Binary
- Given a hexadecimal number, simply convert each digit to it's binary equivalent. Then, combine each 4 bit binary number and that is the resulting answer.

- ## Converting Binary to Hexadecimal
- Begin at the rightmost 4 bits. If there are not 4 bits, pad 0s to the left until you hit 4. Repeat the steps until all groups have been converted.

Binary Arithmetic Operations

- Addition
- Like decimal numbers, two numbers can be added by adding each pair of digits together with carry propagation.

```
  11001
+ 10011
 101100
```

Binary Addition

```
  647
+ 537
 1184
```

Decimal Addition

Binary Arithmetic Operations

- Subtraction
- Two numbers can be subtracted by subtracting each pair of digits together with borrowing, where needed.

```
  11001          627
- 10011        - 537
  -----          ---
  00110          090
```

Binary Subtraction

Decimal Subtraction

Hexadecimal Arithmetic Operations

- Addition
- Like decimal numbers, two numbers can be added by adding each pair of digits together with carry propagation.

```
   5B39
+  7AF4
   D62D
```

Hexadecimal Addition

HexaDecimal Arithmetic Operations

- Subtraction
- Two numbers can be subtracted by subtracting each pair of digits together with borrowing, where needed.

```
   D26F
-  BA94
   17DB
```

Hexadecimal Subtraction

MSB and LSB

- In computing, the **most significant bit (msb)** is the bit position in a binary number having the greatest value. The **msb** is sometimes referred to as the **left-most bit.**

- In computing, the **least significant bit (lsb)** is the bit position in a binary integer giving the units value, that is, determining whether the number is even or odd. The **lsb** is sometimes referred to as the **right-most bit.**

Unsigned Integers

- An unsigned integer is an integer at represent a magnitude, so it is never negative.
- Unsigned integers are appropriate for representing quantities that can be never negative.

Signed Integers

- A signed integer can be positive or negative.
- The most significant bit is reserved for the sign:
  - 1 means negative and 0 means positive.

- Example:

  00001010 = decimal 10

  10001010 = decimal -10

One's Complement

- The one's complement of an integer is obtained by complementing each bit, that is, replace each 0 by a 1 and each 1 by a 0.

2's Complement

- Negative integers are stored in computer using 2's complement.
- To get a two's complement by first finding the one's complement, and then by adding 1 to it.

- Example

```
  11110011     (one's complement of 12)
+ 00000001     (decimal 1)
  --------
  11110100     (two's complement of 12)
```

Subtract as 2's Complement Addition

- Find the difference of 12 – 5 using complementation and addition.
- 00000101 (decimal 5)
- 11111011 (2's Complement of 5)

```
    00001100   (decimal 12)
  + 11111011   (decimal -5)
  ----------
    00000111   (decimal 7)
```

No Carry

Example

- Find the difference of 5ABCh – 21FCh using complementation and addition.
- 5ABCh = 0101 1010 1011 1100
- 21FCh = 0010 0001 1111 1100
- 1101 1110 0000 0100 (2's Complement of 21FCh)

```
   0101 1010 1011 1100 (Binary 5ABCh)
 + 1101 1110 0000 0100  (1's Complement of 21FCh)
 ---------------------
  10011 1000 1100 0000
 ---------------------
```

Discard Carry

Decimal Interpretation

- How to interpret the contents of a byte or word as a signed and unsigned decimal integer?
- Unsigned decimal interpretation
  - Simply just do a binary to decimal conversion or first convert binary to hexadecimal and then convert hexadecimal to decimal.
- Signed decimal interpretation
  - If msb is zero then number is positive and signed decimal is same as unsigned decimal.
  - If msb is one then number is negative, so call it -N. To find N, just take the 2's complement and then convert to decimal.

Example

- Give unsigned and signed decimal interpretation FE0Ch.
- Unsigned decimal interpretation
  - $16^3 * 15 + 16^2 * 14 + 16^1 * 0 + 16^0 * 12 = 61440 + 3584 + 0 + 12 = 65036$
- Signed decimal interpretation
  - FE0Ch = 1111 1110 0000 1100 (msb is 1, so number is negative).
  - To find N, get its 2's complement

0000 0001 1111 0011 (1's complement of FE0Ch)

$\quad$ + $\qquad\qquad\qquad\qquad$ 1

N = 0000 0001 1111 0100 = 01F4h = 500

So, -N = 500

Decimal Interpretation

- For 16 – bit word, following relationships holds between signed and unsigned decimal interpretation
- From 0000h – 7FFFh, signed decimal = unsigned decimal
- From 8000h – FFFFh, signed decimal = unsigned decimal – 65536.
- Example:
- Unsigned interpretation of FE0Ch is 65036.
- Signed interpretation of FE0Ch = 65036 – 65536 = -500.

Binary, Decimal, and Hexadecimal Equivalents.

Binary	Decimal	Hexadecimal		Binary	Decimal	Hexadecimal
0000	0	0		1000	8	8
0001	1	1		1001	9	9
0010	2	2		1010	10	A
0011	3	3		1011	11	B
0100	4	4		1100	12	C
0101	5	5		1101	13	D
0110	6	6		1110	14	E
0111	7	7		1111	15	F

Character Representation

- All data, characters must be coded in binary to be processed by the computer.
- ASCII:
  - American Standard Code for Information Interchange
  - Most popular character encoding scheme.
  - Uses 7 bit to code each character.
  - 2^7 = 128 ASCII codes.
  - Single character Code = One Byte [7 bits: char code, 8th bit set to zero]
  - 32 to 126 ASCII codes: printable
  - 0 to 31 and 127 ASCII codes: Control characters

Dec	Hex	Char	Dec	Hex	Char	Dec	Hex	Char	Dec	Hex	Char
0	00	Null	32	20	Space	64	40	@	96	60	`
1	01	Start of heading	33	21	!	65	41	A	97	61	a
2	02	Start of text	34	22	"	66	42	B	98	62	b
3	03	End of text	35	23	#	67	43	C	99	63	c
4	04	End of transmit	36	24	$	68	44	D	100	64	d
5	05	Enquiry	37	25	%	69	45	E	101	65	e
6	06	Acknowledge	38	26	&	70	46	F	102	66	f
7	07	Audible bell	39	27	'	71	47	G	103	67	g
8	08	Backspace	40	28	(	72	48	H	104	68	h
9	09	Horizontal tab	41	29	)	73	49	I	105	69	i
10	0A	Line feed	42	2A	*	74	4A	J	106	6A	j
11	0B	Vertical tab	43	2B	+	75	4B	K	107	6B	k
12	0C	Form feed	44	2C	,	76	4C	L	108	6C	l
13	0D	Carriage return	45	2D	-	77	4D	M	109	6D	m
14	0E	Shift out	46	2E	.	78	4E	N	110	6E	n
15	0F	Shift in	47	2F	/	79	4F	O	111	6F	o
16	10	Data link escape	48	30	0	80	50	P	112	70	p
17	11	Device control 1	49	31	1	81	51	Q	113	71	q
18	12	Device control 2	50	32	2	82	52	R	114	72	r
19	13	Device control 3	51	33	3	83	53	S	115	73	s
20	14	Device control 4	52	34	4	84	54	T	116	74	t
21	15	Neg. acknowledge	53	35	5	85	55	U	117	75	u
22	16	Synchronous idle	54	36	6	86	56	V	118	76	v
23	17	End trans. block	55	37	7	87	57	W	119	77	w
24	18	Cancel	56	38	8	88	58	X	120	78	x
25	19	End of medium	57	39	9	89	59	Y	121	79	y
26	1A	Substitution	58	3A	:	90	5A	Z	122	7A	z
27	1B	Escape	59	3B	;	91	5B	[	123	7B	{
28	1C	File separator	60	3C	<	92	5C	\	124	7C	|
29	1D	Group separator	61	3D	=	93	5D	]	125	7D	}
30	1E	Record separator	62	3E	>	94	5E	^	126	7E	~
31	1F	Unit separator	63	3F	?	95	5F	_	127	7F	□

How to Convert?

- If a byte contains the ASCII code of an uppercase letter, what hex should be added to it to convert to lower case?
  - Solution: 20 h
  - Example: A (41h) a (61 h)
- If a byte contains the ASCII code of a decimal digit, What hex should be subtracted from the byte to convert it to the numerical form of the characters?
  - Solution: 30 h
  - Example: 2 (32 h)

Character Storage

ASCII Representation of “123” and 123